

# 2.5 Part 1

Monday, June 27, 2022

9:22 AM

## 2.5 Factoring polynomial $ax^2+bx+c$ part 1

Factoring trinomials of the form:  $ax^2+bx+c$  by **Decomposition**

$$\begin{array}{l} \underline{\quad} x \underline{\quad} = (ac) \\ \underline{\quad} + \underline{\quad} = b \end{array}$$

1. Find two numbers who have a product of "ac" and add to "b"
2. Replace the middle term using your two numbers
3. Factor out a GCF from the first pair of terms and another GCF from the second pair of terms
4. Rewrite the trinomial as a product of the common binomial and the remaining terms

**Example 1:** Factor the polynomial by decomposition

a)  $x^2 + 5x + 6$

①  $\begin{array}{l} \uparrow \quad \uparrow \\ (1)(6) = 6 \end{array}$

$$\frac{2}{2} \times \frac{3}{3} = 6$$

$$\frac{2}{2} + \frac{3}{3} = 5$$

factors of 6

$$\begin{array}{l} 1 \times 6 \\ 2 \times 3 \end{array}$$

b)  $f^2 - 2f - 8$

①  $\begin{array}{l} \uparrow \quad \uparrow \\ (1)(-8) = -8 \end{array}$

$$\frac{2}{2} \times \frac{-4}{-4} = -8$$

$$\frac{2}{2} + \frac{-4}{-4} = -2$$

$$\begin{array}{l} -1 \times 8 \\ -2 \times 4 \\ 2 \times (-4) \end{array}$$

②  $x^2 + 2x + 3x + 6$

Replaced 5x with 2x + 3x

$$f^2 + 2f - 4f - 8$$

$$f(f+2) - 4(f+2)$$

③  $x^2 + 2x + 3x + 6$

$$x(x+2) + 3(x+2)$$

$$(f+2)(f-4)$$

④  $(x+2)(x+3)$

c)  $6x^2 + 17x + 5$

①  $\begin{array}{l} \uparrow \quad \uparrow \\ 6(5) = 30 \end{array}$

$$\frac{\quad}{2} \times \frac{\quad}{15} = 30$$

$$\frac{\quad}{2} + \frac{15}{15} = 17$$

$$\begin{array}{l} 1 \times 30 \\ 2 \times 15 \end{array}$$

d)  $2x^2 - 5x - 3$

①  $\begin{array}{l} \uparrow \quad \uparrow \\ 2(-3) = -6 \end{array}$

$$\frac{\quad}{1} \times \frac{\quad}{-6} = -6$$

$$\frac{1}{1} + \frac{-6}{-6} = -5$$

$$\begin{array}{l} -1 \times 6 \\ -2 \times 3 \\ 1 \times -6 \\ 2 \times -3 \end{array}$$

$$6x^2 + 2x + 15x + 5$$

$$2x(3x+1) + 5(3x+1)$$

$$2x^2 + 1x - 6x - 3$$

$$x(2x+1) - 3(2x+1)$$

$$(3x+1)(2x+5)$$

$$(2x+1)(x-3)$$

**Example 2:** Expand using the distributive property to confirm the polynomial has been factored correctly.

a)  $(2x + 7)(x - 3) = 2x^2 + x - 21$

$2x^2 - 6x + 7x - 21$

$2x^2 + 1x - 21$

b)  $(x - 9)(4x - 5) = 4x^2 - 41x + 45$

$4x^2 - 5x - 36x + 45$

$4x^2 - 41x + 45$

Mrs. Shaw

F. & P.-C. 10