

4.1 Linear Approximation

$$L(x) = f'(a)(x - a) + f(a)$$

1. $f(x) = x\sqrt{5-x}$

a) Approximate $f(x)$ by its linearization $L(x)$ at $(1,2)$

b) Graph $f(x)$ and $L(x)$ on the same grid



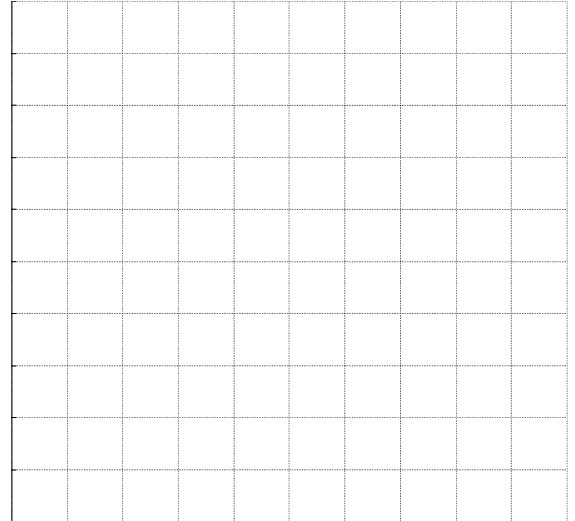
c) Complete the table (use 4 decimal places)

x	0.5	0.9	1	1.1	1.5
f(x)					
L(x)					
L(x) - f(x)					

2. $f(x) = x\sqrt{5-x}$

a) Approximate $f(x)$ by its linearization $L(x)$ at $(4,4)$

b) Graph $f(x)$ and $L(x)$ on the same grid



c) Complete the table (use 4 decimal places)

x	3.5	3.9	4	4.1	4.5
f(x)					
L(x)					
L(x) - f(x)					

3. Which $L(x)$ is a better approximation for $f(x)$ at small equal distances? Explain your answer; refer to data or information you have on this sheet.